

# Fast inversion of hyperspectral observations using Gaussian Locally Linear Mapping

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Mots-clés (5 max.) : Hypersectral data, Atmospheric sounding, Gaussian mixture, Machine learning

Thématique(s) (1 ou 2) : méthodologie, atmosphère

Résumé :

**Background and objective :** The inversion of hyperspectral observations for atmospheric sounding using classical Levenberg-Marquardt (LM) iterative minimization [1] can quickly lead to prohibitive computation time when dealing with observational campaigns that provide a large amount of spatio-temporal data. To significantly improve computational efficiency, we propose to use the machine-learning capabilities of Bayesian inversion techniques.

**Methods :** We simulate noisy hyperspectral data using the 4AOP radiative transfer [2] and the real transfer function of the SCARBO instrument [3] dedicated to monitoring greenhouse gases (GHG) from space. The non-linear forward relationship  $Y=F(X)$  between hyperspectral observations  $Y$  and atmospheric parameters  $X$  is modeled using the Bayesian Gaussian Locally Linear Mapping (GLiMM) approach [4], which constructs a joint probability density  $p(X,Y)$  represented by a Gaussian mixture. The model is learned from a specific training dataset covering the range of admissible atmospheric parameters. The backward model -- that is the probability of having  $X$  knowing the observations  $Y$  -- is then estimated, and the atmospheric parameters of an independent testing dataset are retrieved and compared with their true values.

**Results :** We show that our GLiMM approach retrieves atmospheric parameters a few thousand times faster than iterative LM inversion, while providing similar estimates without significant differences. Considering a 64x64 pixel wide simulated scene with anthropogenic CO<sub>2</sub> emission, we show that the GLiMM process is able to localize the plume with the proper mixing ratio (see Fig. 1) in a few minutes at most.

**Conclusion :** GLiMM modeling is a promising alternative for reliably estimating GHG concentration from a large hyperspectral dataset in a reasonable timeframe.

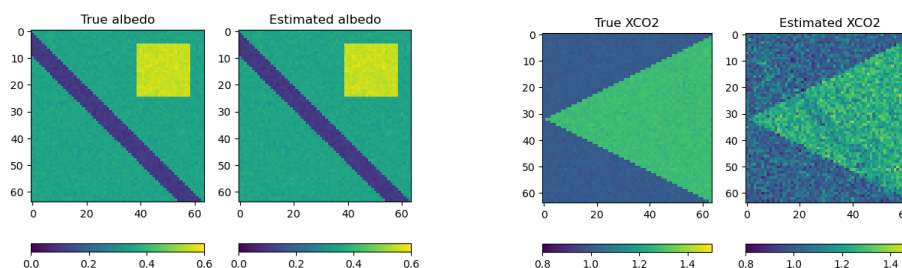


Figure 1 : Comparison of true and GLiMM-estimated albedo (left) and CO<sub>2</sub> mixing ratio (right) parameters for a simulated observation of a spatially localized CO<sub>2</sub> plume.

[1] Rodgers, Clive D. *Inverse methods for atmospheric sounding: theory and practice. Vol. 2.* World scientific, 2000.

[2] Gousset, Silvère, et al. "NanoCarb hyperspectral sensor: on performance optimization and analysis for greenhouse gas monitoring from a constellation of small satellites." *CEAS Space Journal* 11 (2019): 507-524.

[3] Chaumat, L., et al. "4AOP: A fast and accurate operational forward radiative transfer model."

[4] Kugler, B., Forbes, F., & Douté, S. (2022). *Fast Bayesian Inversion for high dimensional inverse problems. Statistics and Computing*, 32(2), 31.